

QUANTUM KEY DISTRIBUTION THE SCIENCE OF SECRET COMMUNICATIONS

Richard J. Hughes
Physics Division
Los Alamos National Laboratory

ABSTRACT

Quantum key distribution (QKD) uses single photon communications to securely transfer cryptographic keys that are required for secure communications. I will describe the theory of QKD and its implementation in both optical fiber and free-space.



Quantum key distribution the science of secret communications

Richard Hughes
Physics Division

Los Alamos National Laboratory

505-667-3876; hughes@lanl.gov; <http://quantum.lanl.gov>

cryptographic key transfer by quantum (single-photon) communications:

- overview of quantum information and cryptography
- the BB84 QKD protocol
- QKD in practice
 - in optical fiber
 - in free-space

Quantum information ?

THEN

- E. Schrödinger, Br. J. Philos. Sci. III,
August 1952:

“...we never experiment with just one electron or atom or (small) molecule.

In thought experiments we sometimes assume that we do; this invariably entails ridiculous consequences. ... In the first place it is fair to state that we are not experimenting with single particles, any more than we can raise Ichthyosauria in the zoo.”

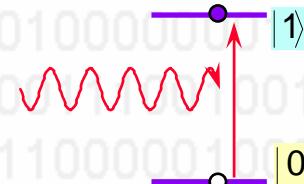
and NOW

- “... it seems that the laws of physics present no barrier to reducing the size of computers until bits are the size of atoms, and quantum behavior holds sway.” R. P. Feynman (1985)

Quantum bits = “qubits”

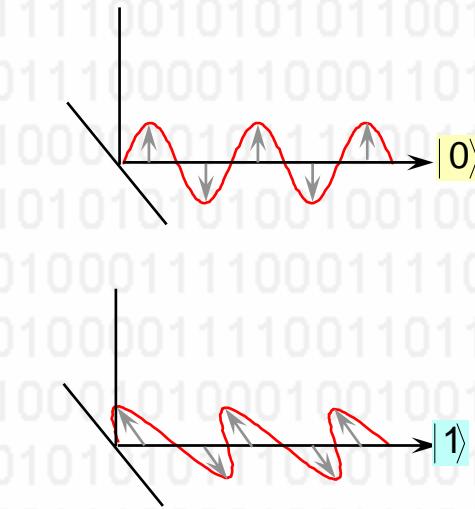
- a single bit of information can be represented by a two-state quantum system

- a “qubit”



- an atomic electron

- a polarized photon



- a spin in a magnetic field

QUANTUM CRYPTOGRAPHY: PUBLIC KEY DISTRIBUTION AND COIN TOSSING

Charles H. Bennett (IBM Research, Yorktown Heights NY 10598 USA)

Gilles Brassard (dept. IRO, Univ. de Montreal, H3C 3J7 Canada)

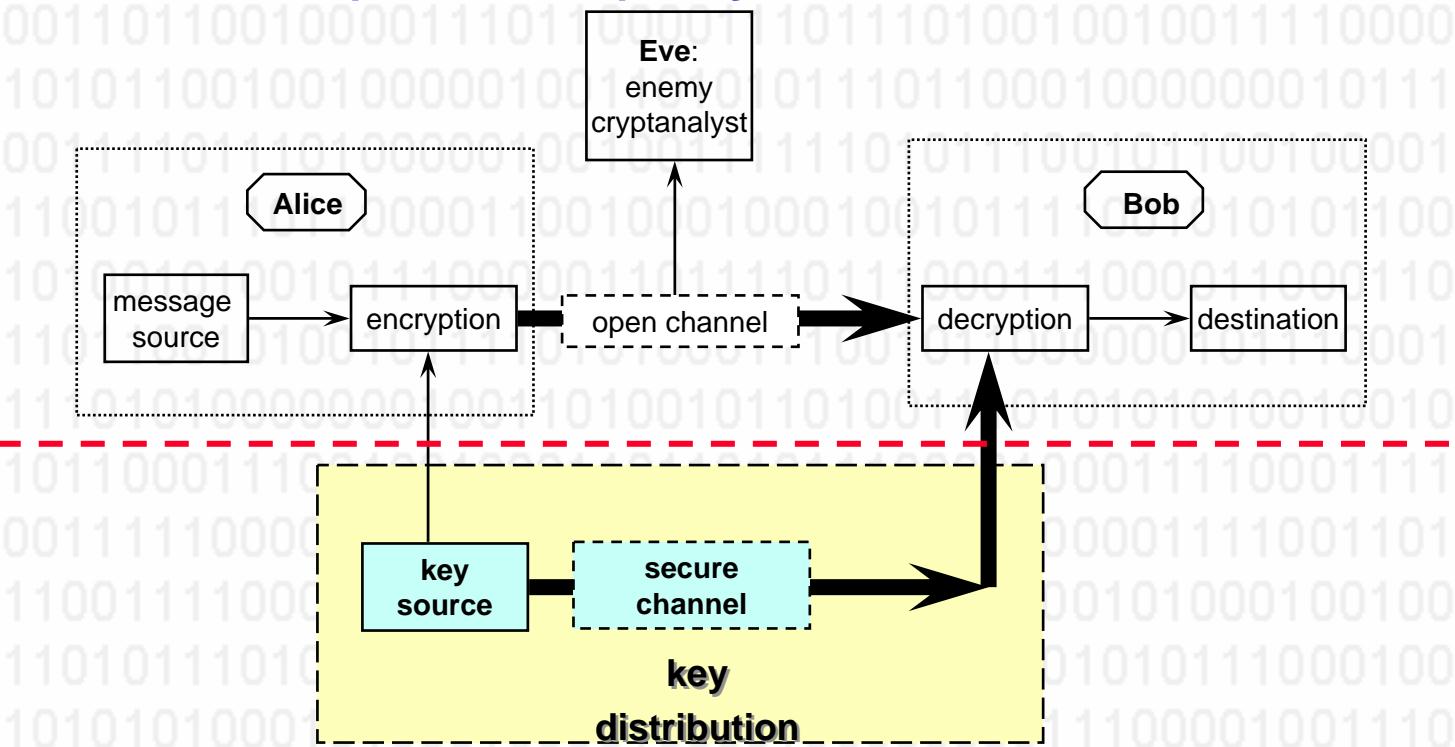
International Conference on Computers, Systems & Signal Processing, Bangalore, India December 10-12, 1984

“When elementary quantum systems ... are used to transmit digital information the uncertainty principle gives rise to novel cryptographic phenomena unachievable with traditional transmission media.” (1984)

first commercial (fiber) QKD systems: 2003



(Quantum) Key Distribution



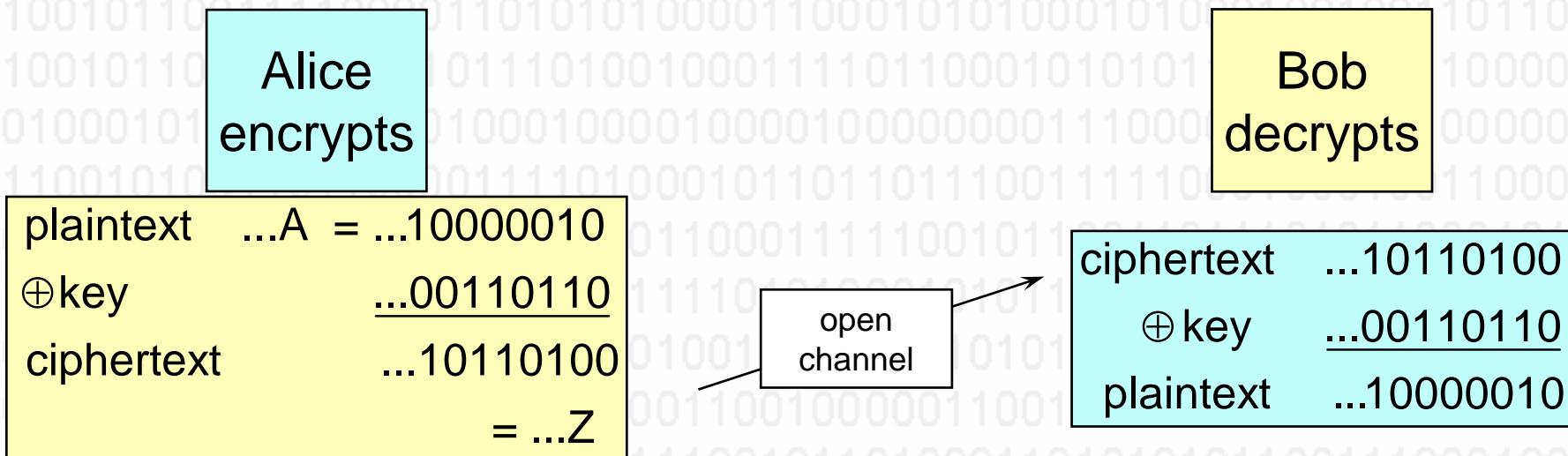
- quantum key distribution = on-demand key transfer by quantum communications
- detectability and defeat of eavesdropping ensured by laws of physics & information theory
- avoids latent vulnerability of public key broadcasts, and advent of quantum computers
 - passive monitoring ineffective
 - “today’s quantum cryptography transmissions not vulnerable to tomorrow’s technology”
- reduces insider concerns: key material does not exist until transmission time
- compatibility with optical communications/existing & planned infrastructures

Secrecy: the “one-time pad”

G. S. Vernam, Trans AIEE 45, 295 (1926)

- key material is a (truly) random bit sequence

- XOR= \oplus = addition (mod 2) = binary addition without carry
- unconditionally secure
 - provided key is not reused
 - key is as long as the message

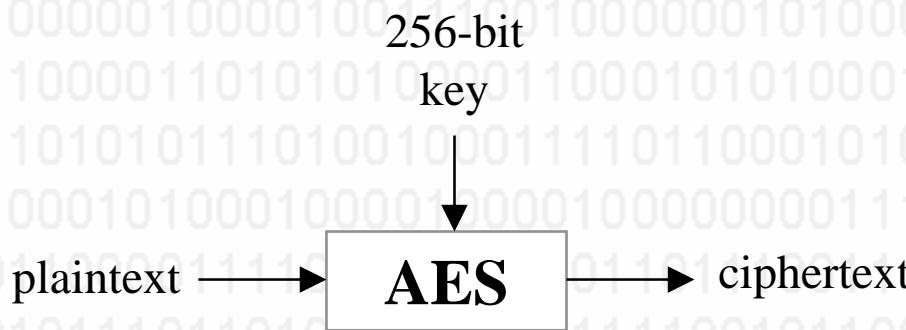


for surveys on confidentiality and authentication, see

“Contemporary Cryptology” G. J. Simmons ed., IEEE (1992)

Practical secrecy: symmetric key cryptography

- “**practical secrecy**”: “**very, very hard to break, and thoroughly analyzed**”
 - e.g. NIST’s Advanced Encryption Standard, AES



Quantum Key Distribution (QKD) is evolving along dual tracks:

Shannon (1949): “theoretical secrecy” & “practical secrecy”

theoretical secrecy

Bennett-Brassard 1984

authentication + quantum
communications +
information theory = QKD

practical secrecy

computational security

influx

heritage

QKD today

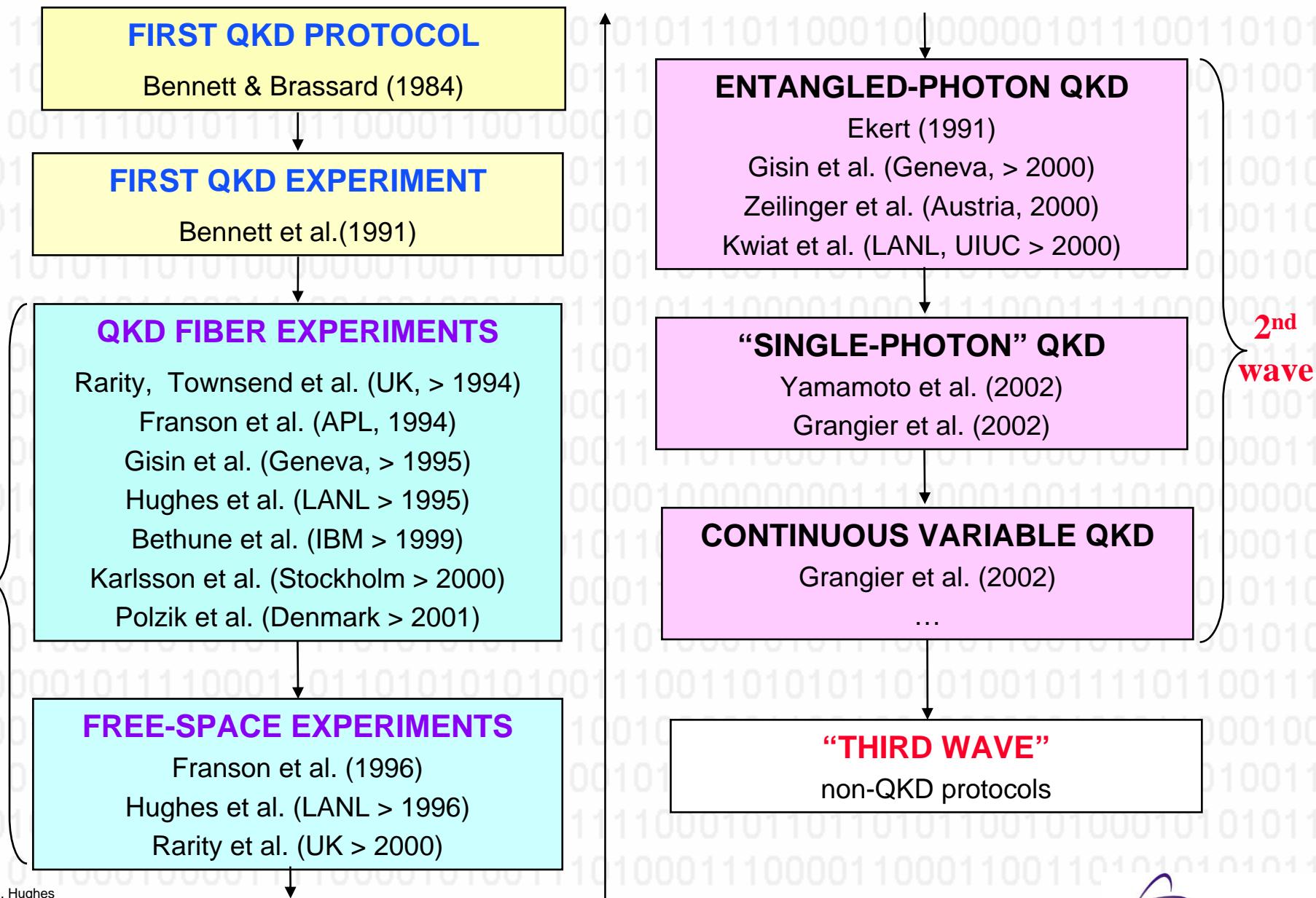
new security
paradigm

capability
enhancement ?

“unconditional security”

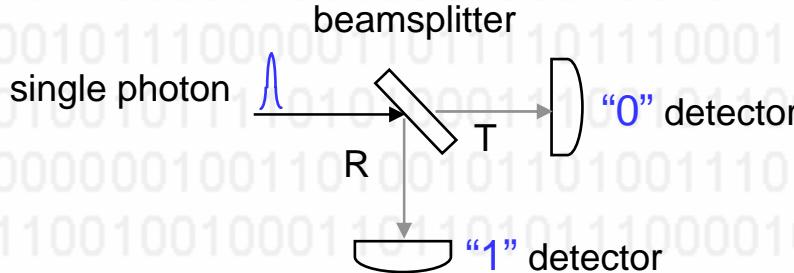
future secure
communications needs

QKD (“1st and 2nd waves”)



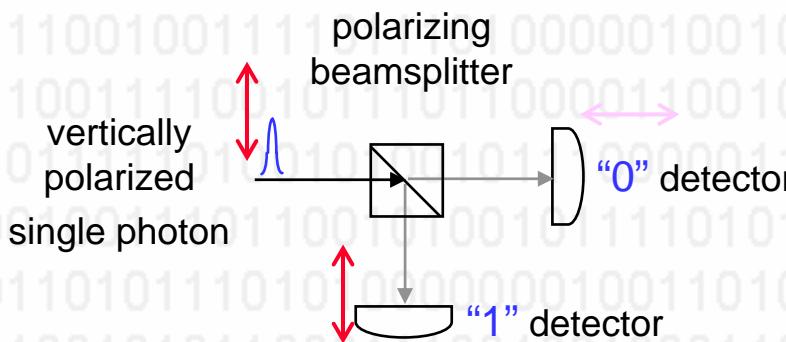
Quantum mechanics of ideal single photons & detectors

- a single photon cannot be split

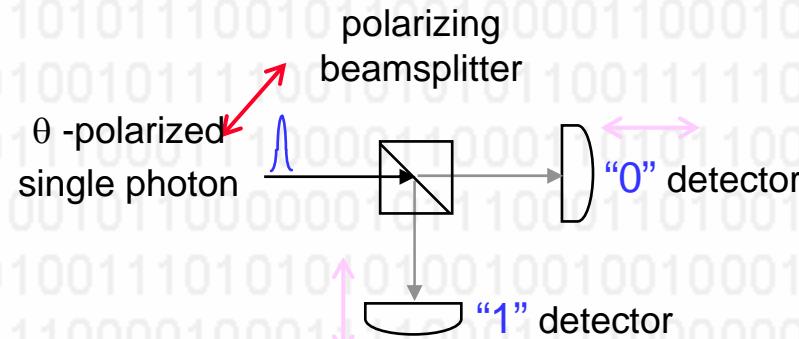


- **EITHER** detector "0" **fires OR** detector "1" **fires**
 - not both
 - we cannot predict, even in principle, which detector will fire
 - irreducible randomness of quantum physics

Quantum mechanics & (linearly) polarized single photons



- detector “0” never fires
- detector “1” always fires



- detector “0” fires with prob = $\cos^2\theta$
- OR, “1” fires with prob = $\sin^2\theta$
 - not both
 - we cannot predict which one

implications

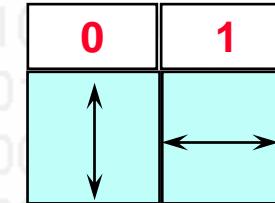
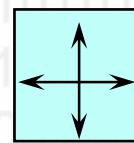
- orthogonal polarization can be distinguished
- non-orthogonal polarizations cannot be faithfully distinguished
- after **measurement** a photon has no “memory” of its prior polarization
- **[non-orthogonal polarizations cannot be faithfully copied (“no cloning”)]**

“Conjugate coding”

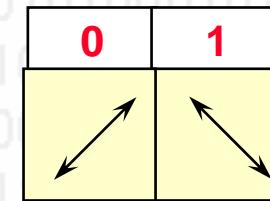
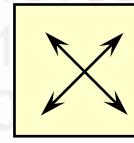
S. Wiesner, SIGACT News 15(1), 78 (1983)

- a bit of information can be encoded in orthogonal polarization states of single photons, in different bases:

- e.g. in the rectilinear basis



- in the diagonal (45°) basis (“conjugate”)

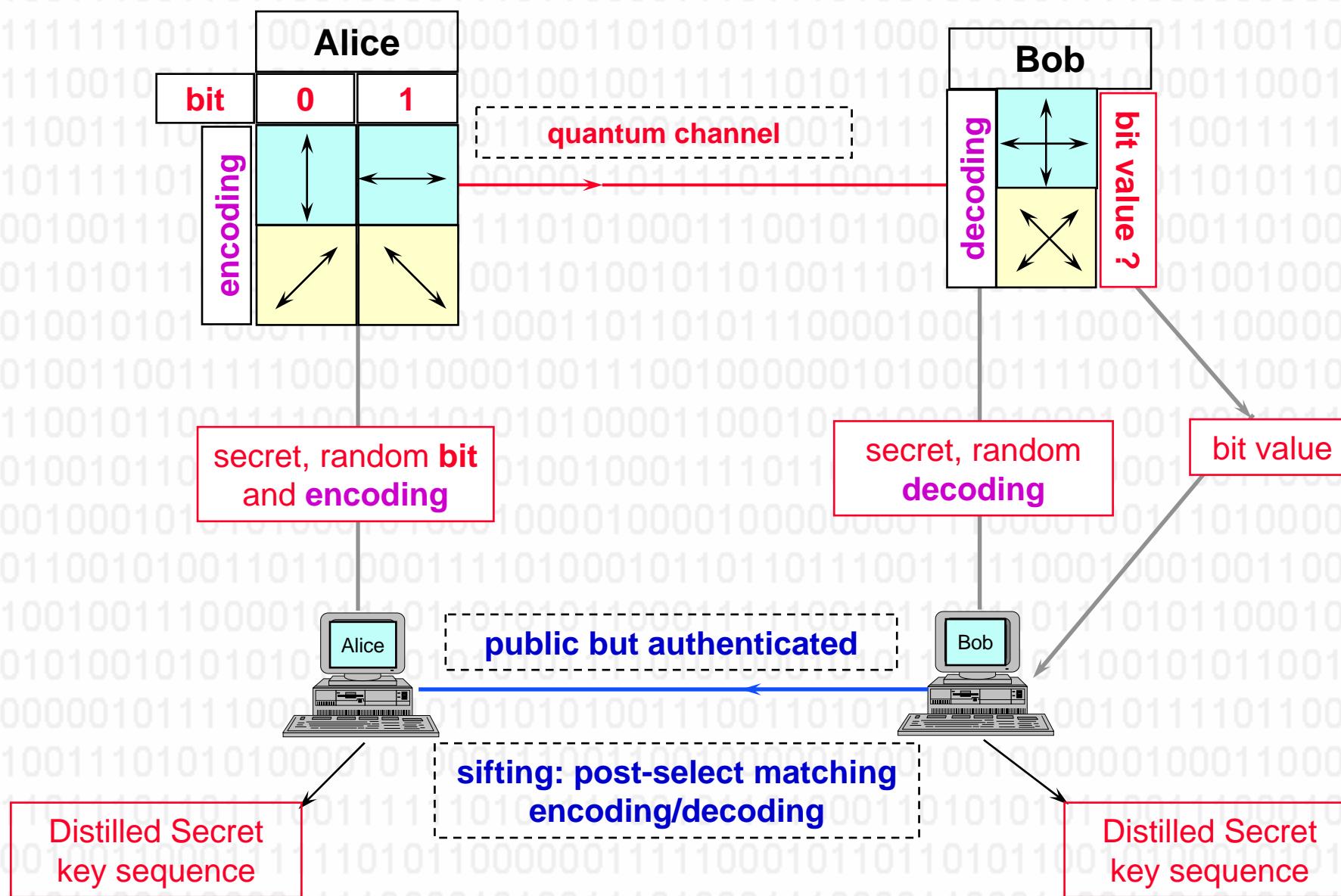


- the bit can be faithfully decoded if the encoding basis is known
- if the wrong decoding basis is used, the outcome is random

The core ingredients of the BB84 QKD protocol (I)

- Alice has two sources of random bits
 - long-term secret data bits
 - independent, short-term secret encoding bits
- Bob has an independent source of short-term secret random decoding bits
 - they have a quantum channel
 - allows the faithful transmission of polarized single photons
 - they have a means to perform conjugate encoding and decoding
 - ideal single photon sources and detectors
 - they have an authenticated, but non-secret, conventional public channel
 - they know they are communicating with each other, and not an impersonator (“Eve”)
 - they know that Eve has not substituted her own messages

Core ingredients of the BB84 (QKD) Protocol (II)



An example of BB84

Alice data bit	1	0	0	0	1	1	0	1
Alice basis								
A → B quantum								
Bob basis								
Bob detects	1	0/1	0	0/1	0/1	0/1	0	1
B → A public	R	D	D	D	R	R	D	R
A → B public	Yes	No	Yes	No	No	No	Yes	Yes
sift	1		0				0	1

- Alice and Bob now share 4 random (“sifted”) bits

Points to note

From Alice and Bob's perspective:

- on average the protocol is 50% efficient
- Alice and Bob cannot predict which bits they will share
 - sifted key is a random sequence of random bits
- only photons that arrive can enter the sifted key
 - photon loss reduces the key rate
- in practice other photons may enter the quantum channel
 - source of errors ?

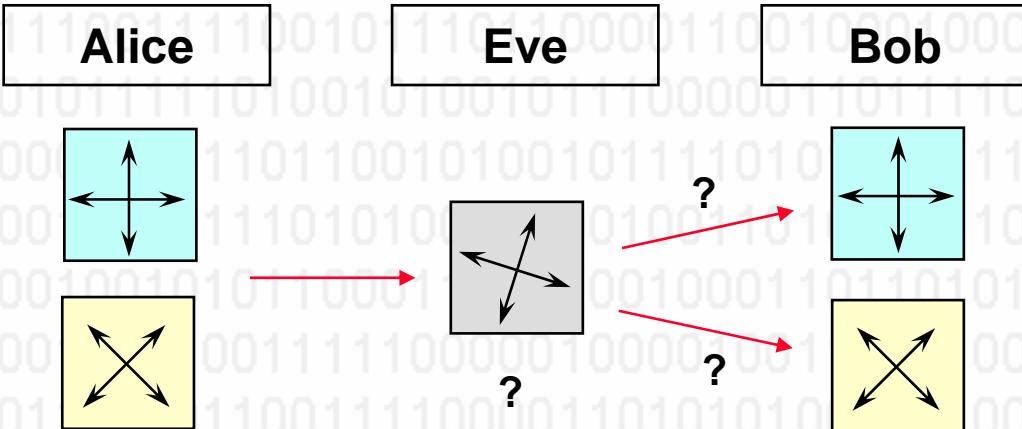
From Eve's perspective

- cannot passively monitor the quantum channel: a photon cannot be split
 - no possibility of storing information for future analysis
- public channel conveys no information about the (secret) data bits
 - cannot perform a man-in-the-middle attack
 - public channel is authenticated
- use quantum physics methods to distinguish the quantum channel states?

(Intercept-resend) eavesdropping on QKD ?

C. H. Bennett et al., J. Crypto 5, 3 (1992)

- Eve inserts a polarizer at angle θ ?



e.g. Alice sends "V", Eve tests " θ "

- $P(\text{Eve correct}) = \cos^2\theta$
- sends Bob θ
- $P(\text{Eve wrong}) = \sin^2\theta$
- sends Bob $(90^\circ - \theta)$

- e.g: Eve tests randomly in the rectilinear and diagonal bases: on average
 - learns 50% of Alice's bits
 - has 50% bit error rate (BER) on the rest
 - once she learns the basis information

• impacts:

- Eve can only gain partial information**
 - deterministic or probabilistic
- necessarily causes a disturbance**
 - Bob has a 25% BER if Eve tests every bit**

Bisective search interactive error correction: “BINARY¹”

Alice

1 1 0 1 1 0 0 0 1 0 1 1

$A \rightarrow B : \oplus = 1$

1 1 0 1 1 0

0 0 1 0 1 1

$A \rightarrow B : \oplus = 1$

1 1 0 1 1 0

$\oplus = 0$

1 1 0

$\oplus = 0$

1 1

$\oplus = 1$

1

Bob

1 1 0 1 0 0 0 0 1 0 1 1

$\oplus = 0$

1 1 0 1 0 0

0 0 1 0 1 1

$\oplus = 1$

1 1 0 1 0 0

$\oplus = 1$

1 0 0

$\oplus = 1$

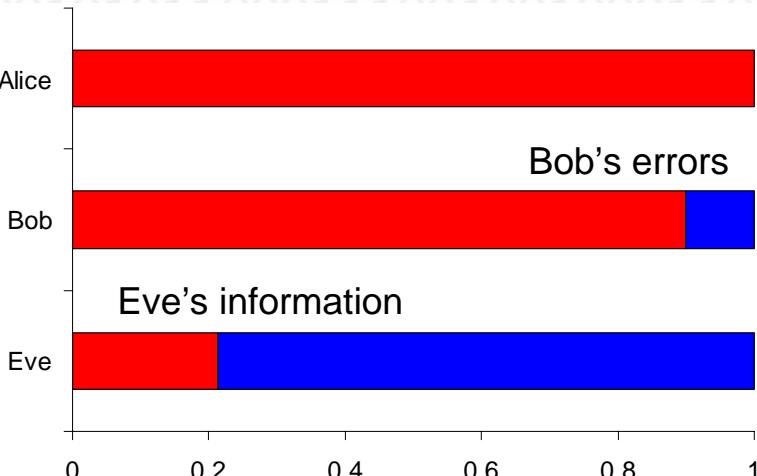
1 0

$\oplus = 0$

X → 1

Eavesdropping on QKD can be detected and defeated

- Eve may only obtain partial information by testing Alice's photons
- and at the price of introducing errors into Bob's key:



- Alice and Bob can upper bound Eve's information after error correction

- using "privacy amplification" Alice and Bob produce a shorter, secret key:

- e.g. Alice and Bob have 6 bits:

a, b, c, d, e, f

- they KNOW Eve knows 3 bits, but not which three

- they can extract 2 SECRET bits:

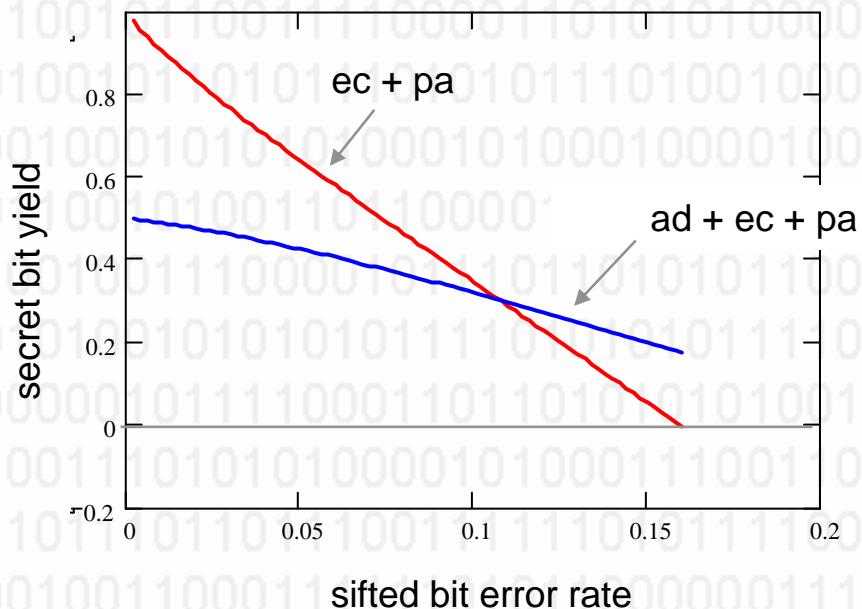
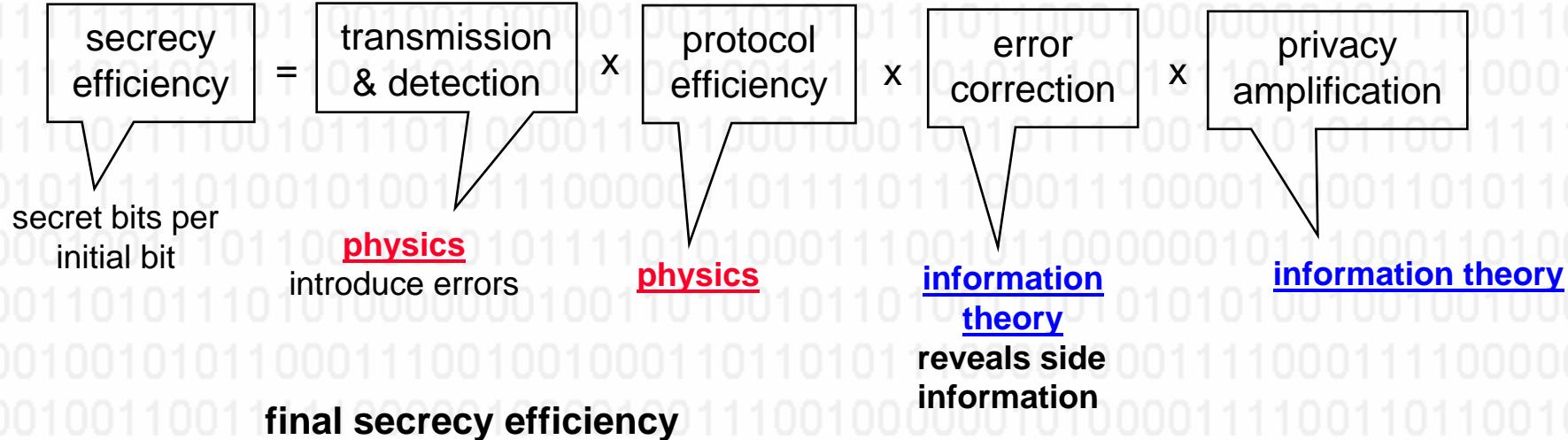
a⊕b⊕c⊕d and **c⊕d⊕e⊕f**

- privacy amplified bits are unknown to Eve:

- can be used for cryptography

C. H. Bennett et al., IEEE Trans Inf Th. 41, 1915 (1995)

QKD link equation: an interplay between quantum physics and information theory



security attributes
 either: defeat eavesdropping (up to a point)
 or: failsafe (eavesdropping becomes DoS)
NB. tolerant of high quantum BERs

QKD may **not** be possible EVEN IF photons can be transmitted and detected

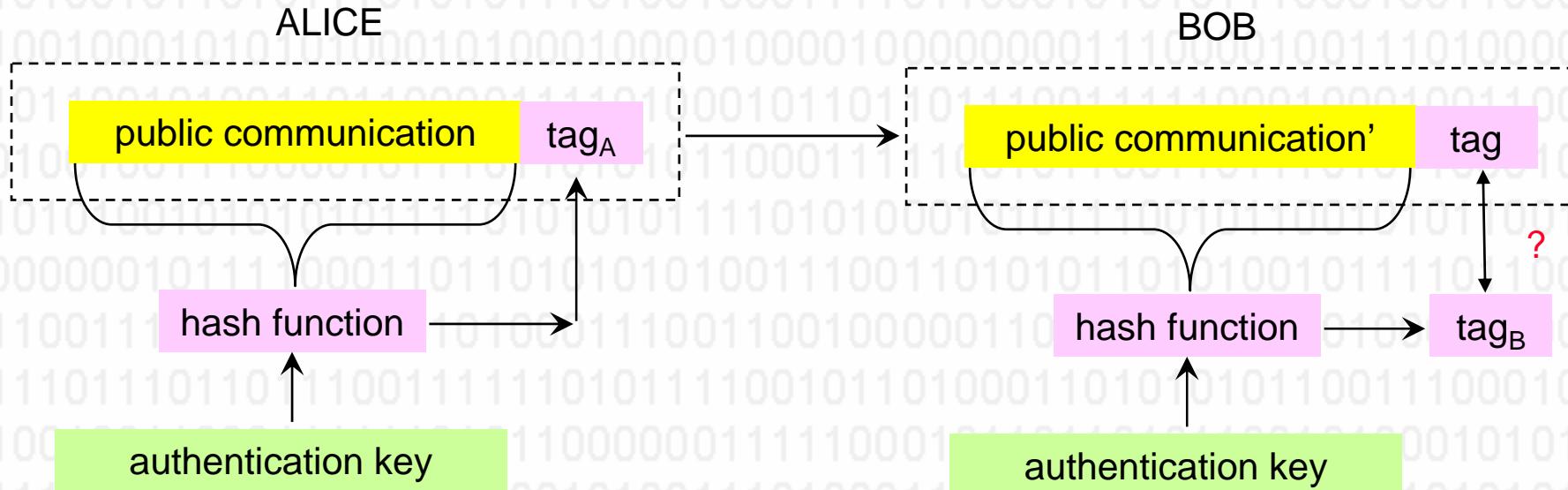
LA-UR-04-8691

Unconditionally-secure Wegman-Carter authentication

M. Wegman and J. Carter, J. Comp Sys Sci 22, 265 (1981)

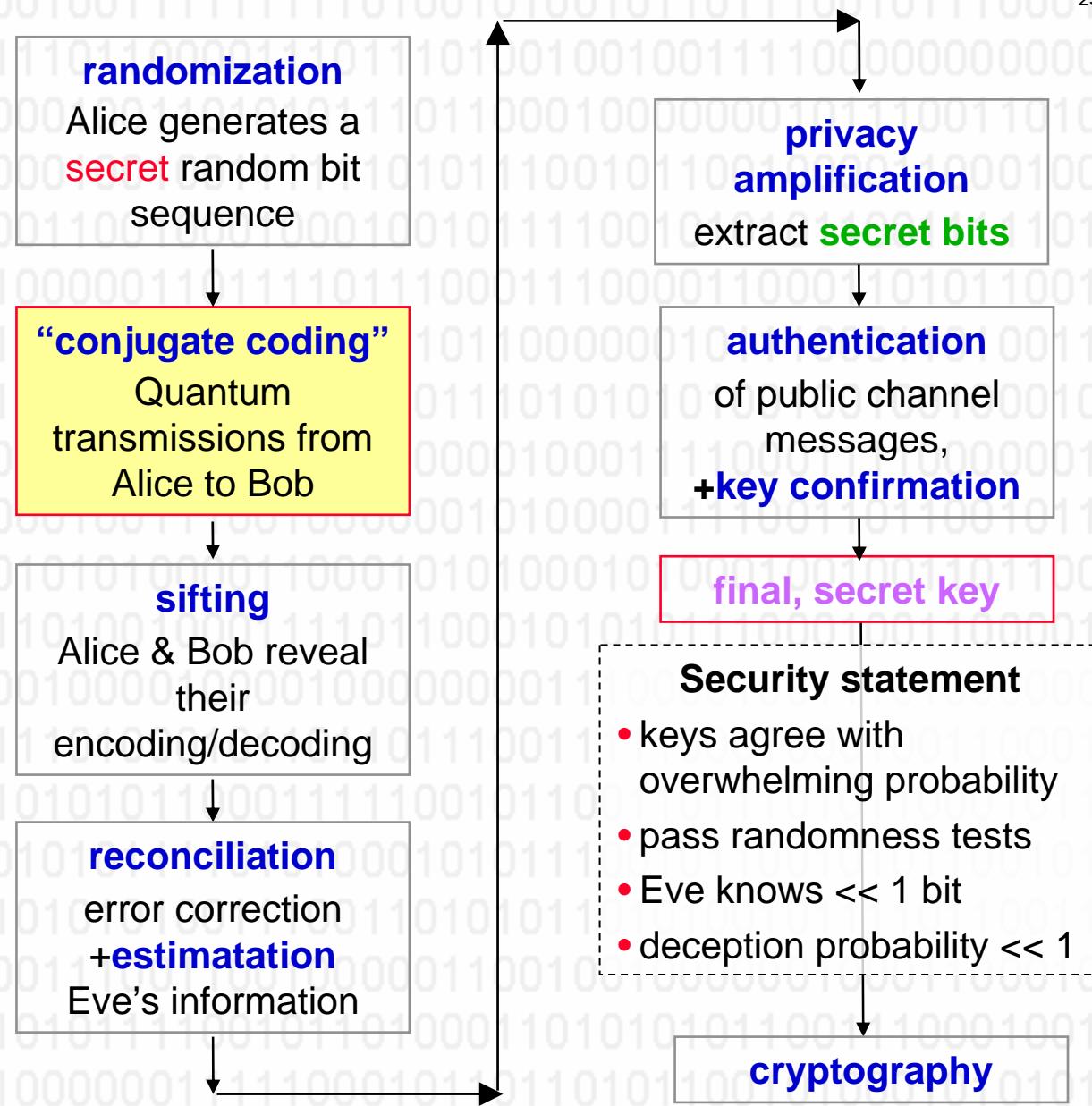
- protection against “man-in-the-middle” ?

- Alice must know she is talking with Bob, and vice-versa
 - impersonation by Eve ?
- authentication of public channel communications
 - substitution by Eve ?
- Alice and Bob share a short (short-term) secret authentication key
 - compute a keyed hash; apply as authentication tag to messages
 - “cost” is small: logarithmic in # bits authenticated**



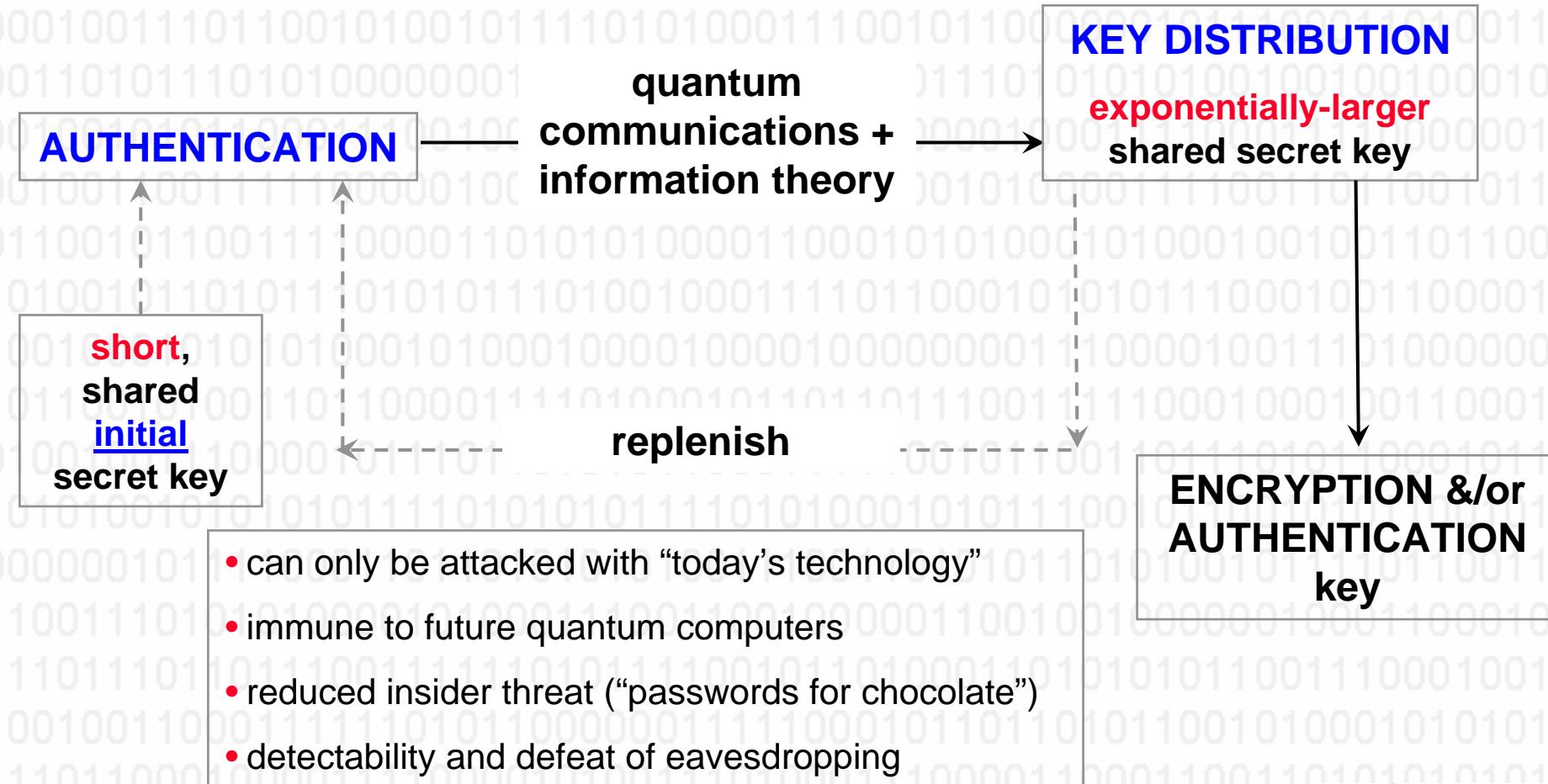
NECESSARY INGREDIENTS of QKD

- cryptographic quality random bits
- quantum comm.
- sifting
- error correction
- bound on information leakage
- privacy amplification
- authentication
- key confirmation
- randomness tests
- standards



What does QKD offer ?

- “from **one-time authentication** to **self-sustaining** key distribution”
 - drastically narrows an adversary’s scope & window of opportunity:
 - must break initial authentication in real-time and attempt an invasive “man-in-the-middle” attack ?



Practical light sources, quantum channel & photon detectors

"single photon"
= weak Poissonian

$$P(n) = \frac{e^{-\mu} \mu^n}{n!}$$

$$\langle n \rangle = \mu < 1$$

sometimes send > 1 photon: security ?

detector efficiency = η

$$P_D = (1 - e^{-\mu\eta})$$

sometimes don't detect it

$$P(n) = \frac{e^{-\mu} \mu^n}{n!}$$

$$P(n) = \frac{e^{-T\mu} (T\mu)^n}{n!}$$

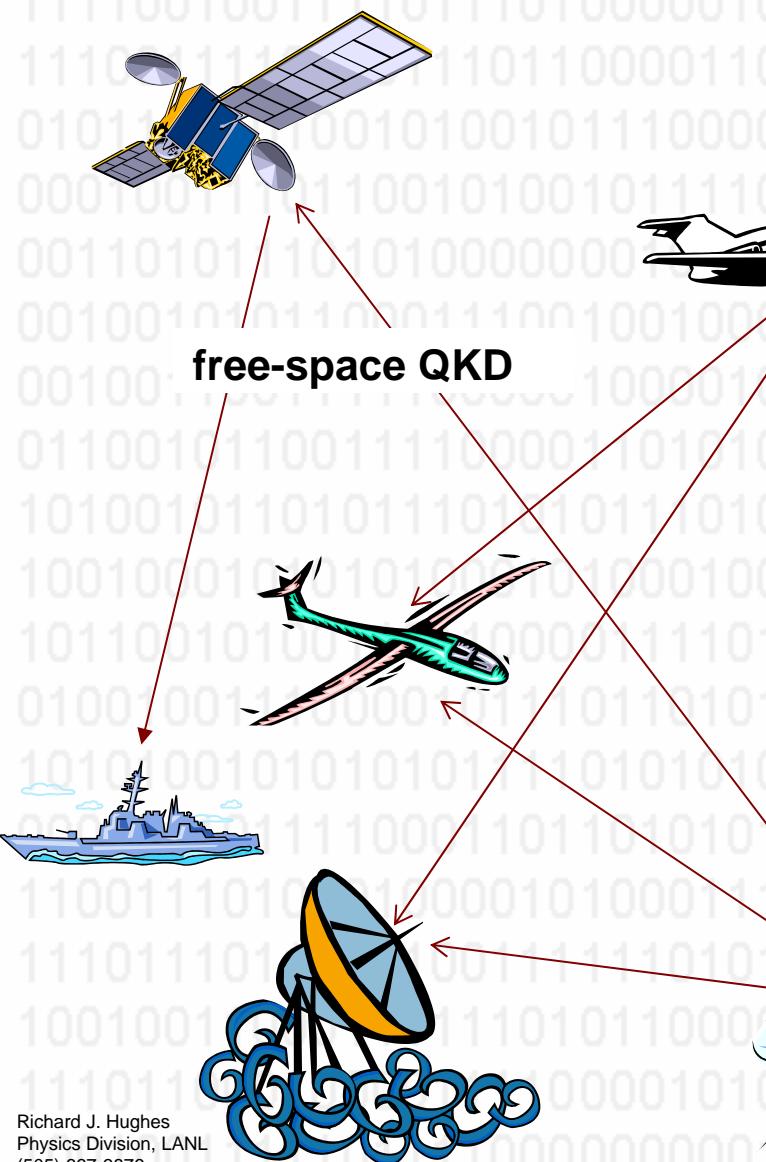
$$\langle n \rangle = T\mu$$

"loss" = random partitioning

- no-photon fraction and loss make it harder for Alice and Bob
- multi-photon fraction & noise introduce new opportunities for Eve
- revised privacy amplification
- secret bit rate ?

Line-of-sight (“free-space”) QKD would be especially useful

R. J. Hughes and J. E. Nordholt, Physics World, May 1999, 31.



- possible today at practical rates with COTS+ technology

- **QKD is robust**

- **large losses (20-30dB) and v. high BERs (% range) can be tolerated**

- **availability**

- **comparable to conventional laser comm.**

secure enclave

optical fiber QKD

The atmospheric QKD quantum channel

low-loss transmission wavelength; high-efficiency detectors

J. E. Nordholt et al., Proc SPIE 4635, 116 (2002)

- **secrecy efficiency as a function of wavelength:**

- ~ 780 nm is optimal for QKD through the atmosphere

- single-photon detection with Si APDs

- **challenges**

- **background photons**

- daylight radiance $\sim 10^{13}$ photons $s^{-1} cm^{-2} \text{\AA}^{-1} sr^{-1}$

- $\sim 10^{-7}$ photons mode $^{-1}$

- temporal filtering: ~1 ns

- spectral filtering: 0.1 nm

- spatial filtering: 220- μ rad FOV

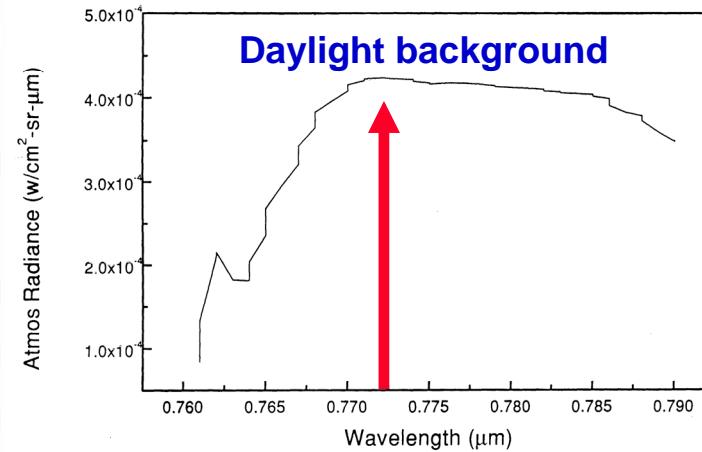
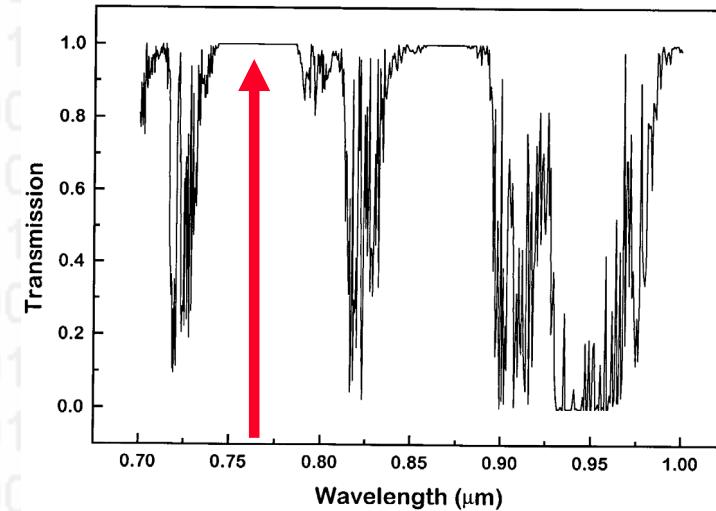
- **day/night $\sim 10^6$**

- **synchronization and timing**

- **atmospheric optics ?**

- not birefringent; intermittency: ~ 0.01-s

Atmospheric transmission
vs. wavelength



Free-space quantum key distribution

R. J. Hughes et al., New Journal of Physics (www.njp.org) 4, 43.1-43.14 (2002)



Sample of key material at 10-km range (day)
one-airmass path: comparable optics to satellite-to-ground

A: 01110001 0111010 0010001 01100100 10100110

B: 01110001 0111010 0010001 01100100 10100110

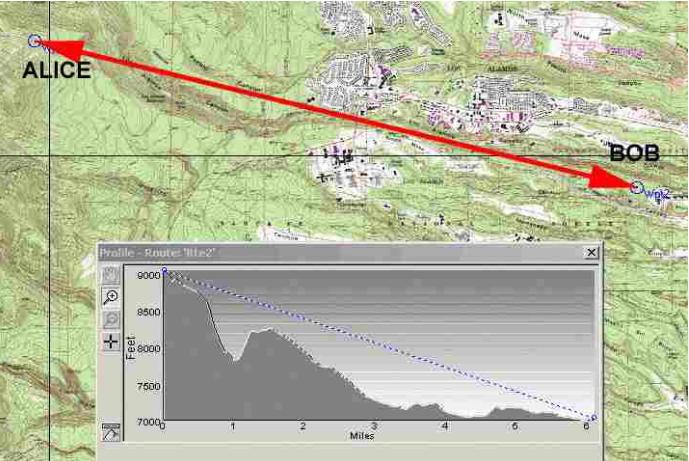
A: 11100010 00111101 10011111 10000111 11001111

B: 11100010 00111101 10011111 10000111 11001111



- key transferred by 772-nm single-photon communications
- 1-MHz sending rate; ~600-Hz key rate
- day: 45,576 secret bits/hour ; night: 113,273 secret bits/45 mins

Receiver "Bob"



From Pajarito Mtn., Los Alamos, NM to
TA53, Los Alamos National Laboratory

Richard J. Hughes



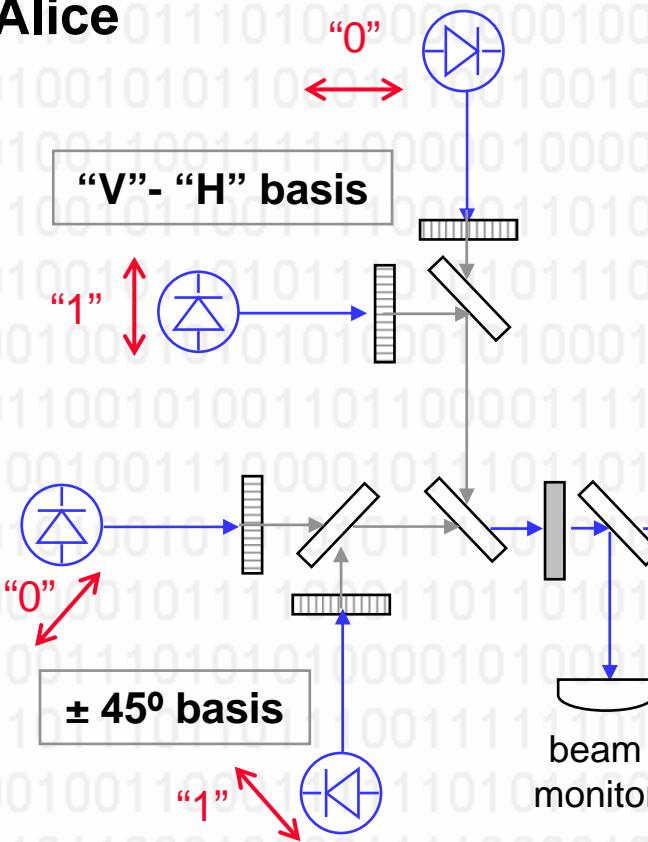
Pajarito Mountain
Ski Area

Los Alamos
NATIONAL LABORATORY

BB84 subsystem

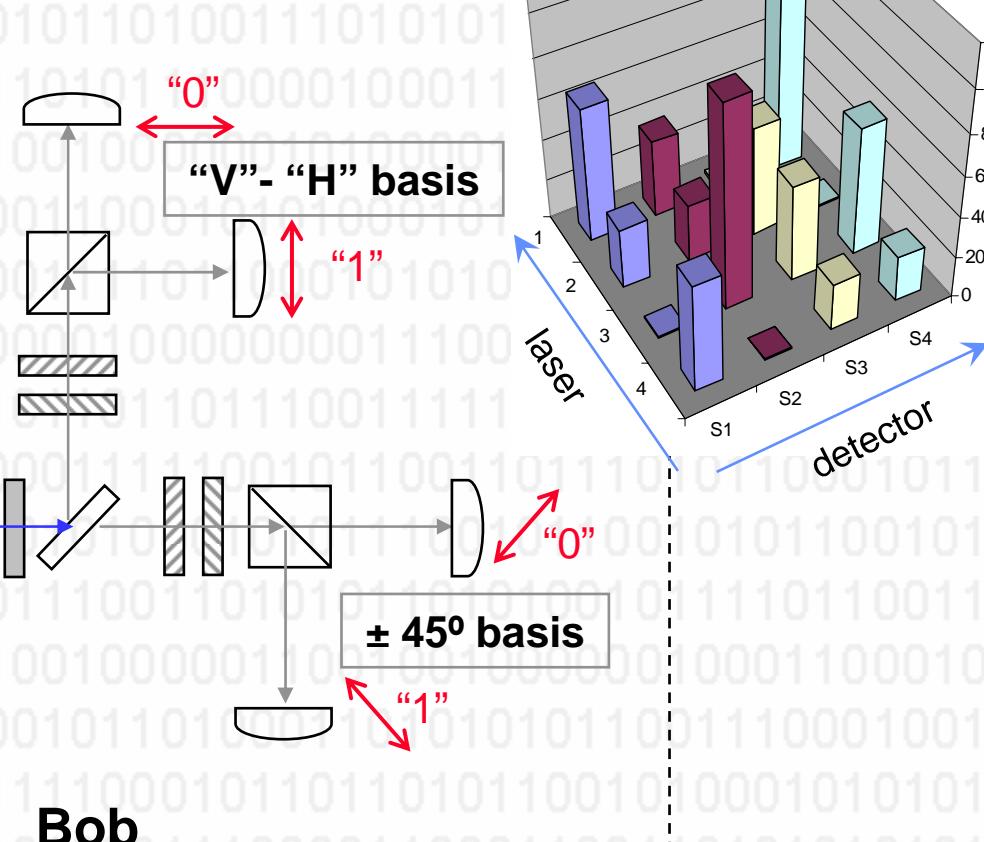
- monolithic randomizer chip
 - 2-MHz clock rate → 1-MHz signal rate
- BB84 photons: attenuated 772-nm lasers
 - 1-s quantum transmissions

Alice



- single-photon detectors: cooled Si APDs
 - passive quench; $\eta \sim 61\%$; dead time $\sim 1 \mu\text{s}$
- quantum random number generation
- multi-detector system: upper bound on multi-photon pulses

Bob

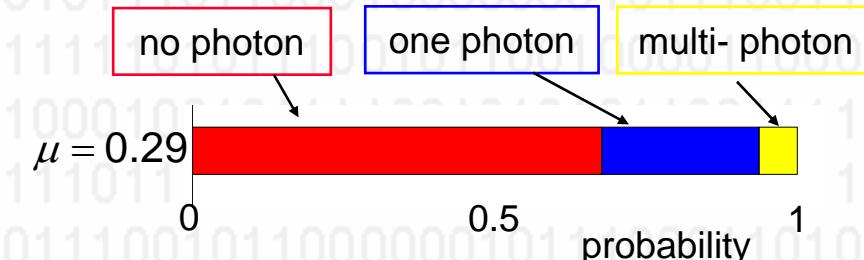


From sifted bits to secret bits

e.g. in daylight from 18:40:26 - 18:40:27 MDT 4 October, 2001

In 1 s, from 10^6 transmitted bits with
photon number $\mu = 0.29$ Alice and Bob
produce **651 (partially secret) sifted bits**
with **21 errors** (BER, $\varepsilon = 3.2\%$):

```
000001100110001001000001011010000110011100100011111000010  
001111001011001000101001100110001010110110110111110  
0010101001111100111111011110110111100001010010001  
0010101100011011000010110000100101110010100111001010011  
1110111001100001110001000011011000111100010100100010  
011000110010110011110111111000001111011011001100011100  
1011010011010011101010001010110000101000111011011  
110011101101111010011111001100101101001110001110010101  
00101000001101111001001000100111110111100100110100011100  
11110011011000100010101110110000111111010110  
111101000001110011001011011100000111111010110  
00011000010101110010110110010110110
```



BBBSS91 privacy amplification^[1]

Eve's entropy >

651 bits

- **171 bits (multi-photon)**

- **40 bits (intercept-resend)**

- **155 bits (side information: error correction)**

- **2 bits (side information: bias)**

- **20 bits (“safety factor”)**

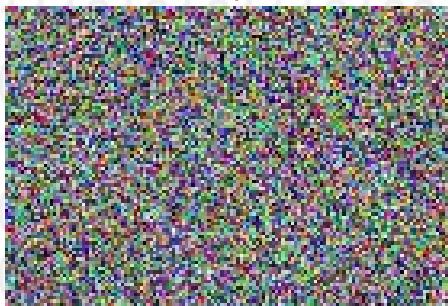
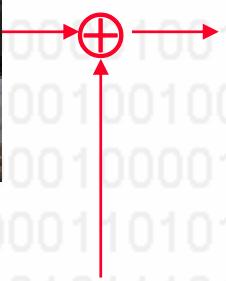
= **264 bits (secret)**

Eve's expected information < **10^{-6} bits**

[1] C. H. Bennett et al. J. Crypto 5, 3 (1992)

One-time pad encryption of an image using final key (error correction, privacy amplification & check)

Encrypted Image



Alice encrypts

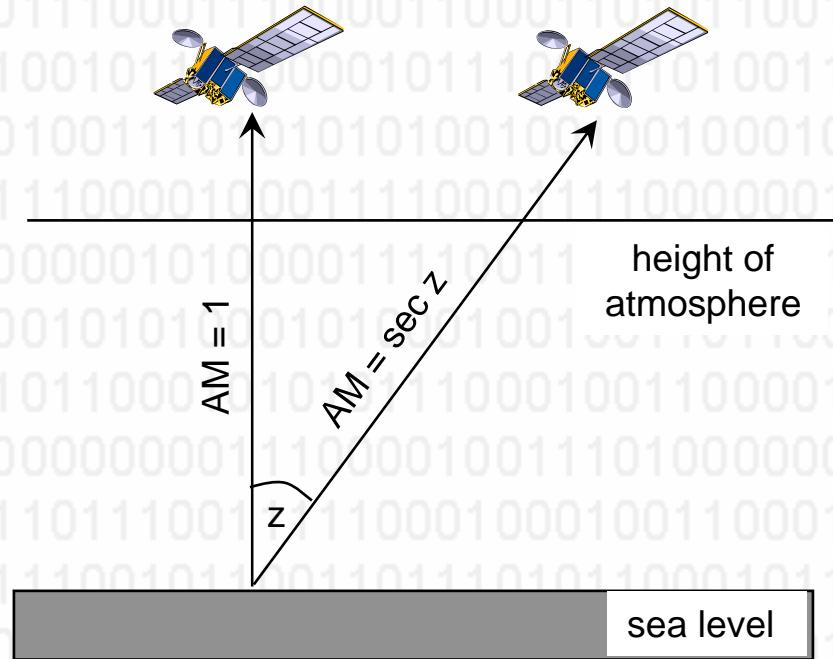
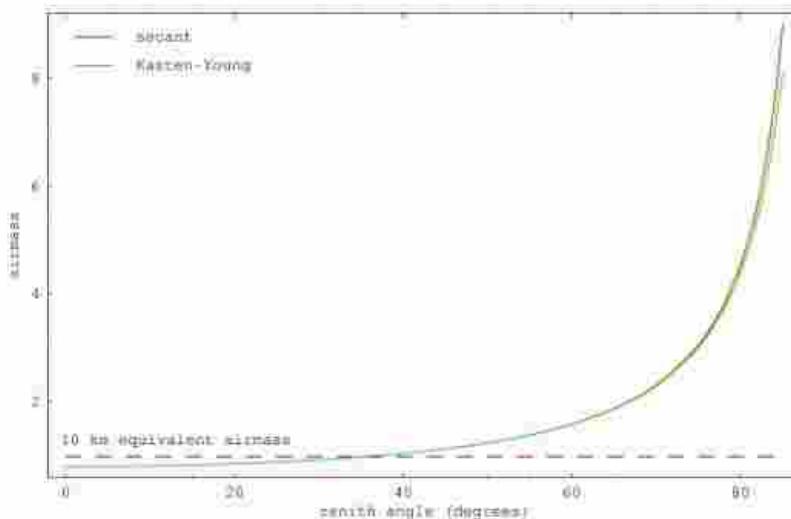
**by adding a word of
her key
to each pixel**

Bob decrypts

**by subtracting a
word of his key
from each pixel**

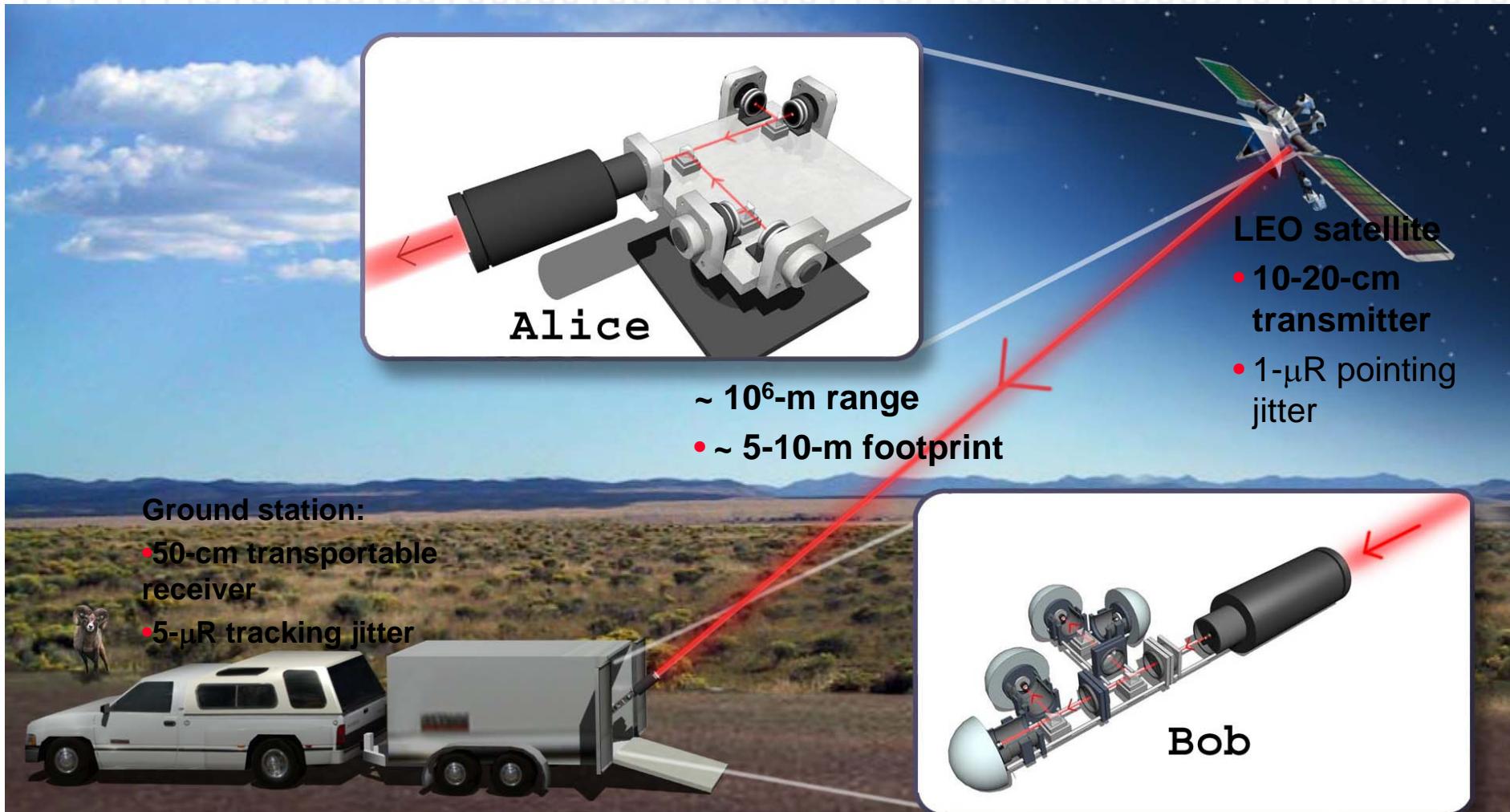
Atmospheric optics of 10-km path

- 10-km path has **extinction** (1 AM), **background** and **capture efficiency** comparable to a path to space
 - “airmass”: a measure of atmospheric extinction (and “seeing”)
 - zenith path from Los Alamos has ~ 0.8 AM



QKD with LEO Satellites Possible with Small Terminals

J. E. Nordholt et al., Proc SPIE 4635, 116 (2002)



Ground station:

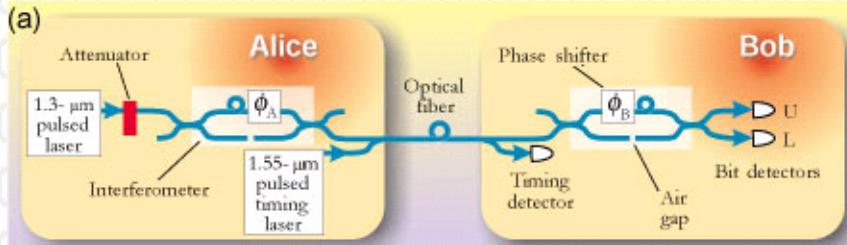
- 50-cm transportable receiver
- 5- μR tracking jitter

availability: rates ~ “100s secret keys/contact minute/notional day” feasible

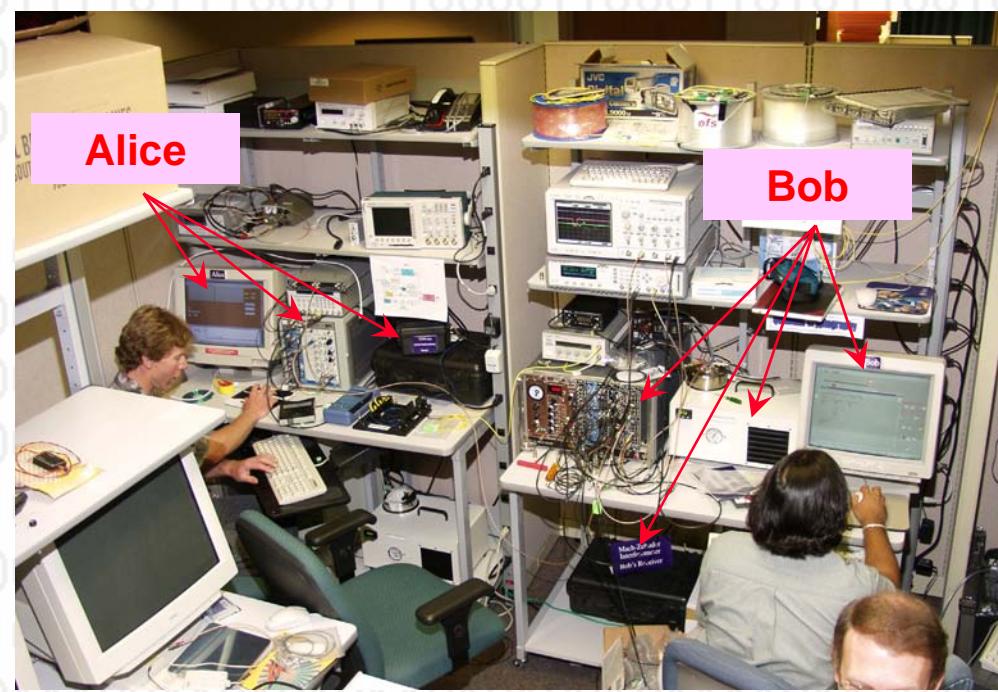
QKD in optical fiber: e.g. previous LANL QKD systems designed for dark fiber

R. J. Hughes et al., LNCS 1109, 329 (1996)

F1QKD (@ LANL > '95)



F2QKD (@ FtMeade > '97; LTS > '02)



held distance records for multiple years, but not network- (or user-) friendly ...

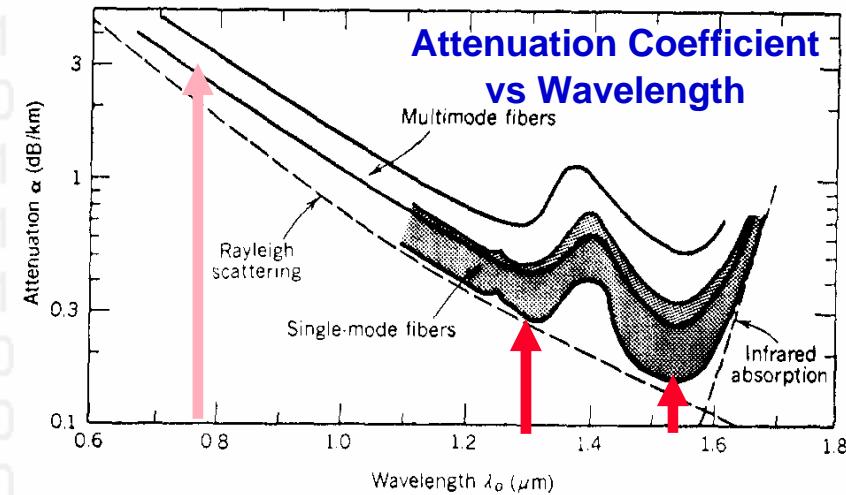
- the challenge for fiber-based QKD: “co-existence” in an active optical network ... LANL next-generation system: “Fiber III”

The QKD Quantum Channel

low-loss transmission medium; high-efficiency detectors

- optical fiber

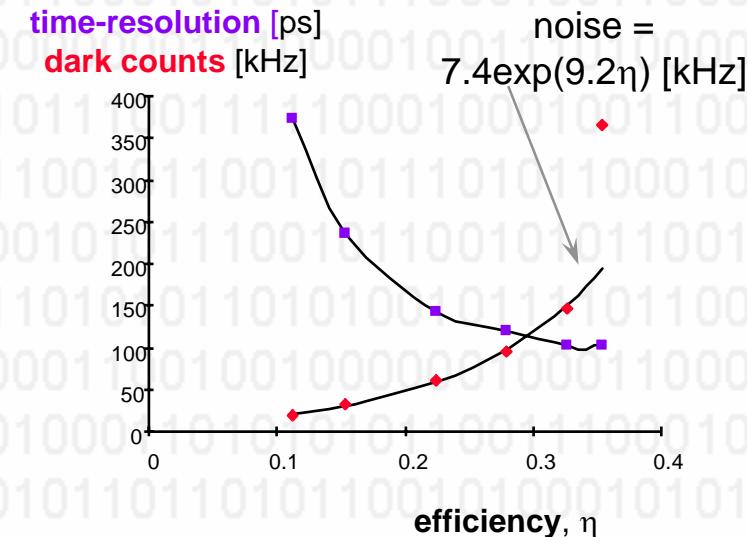
- QKD over telecommunications fiber networks ?
- challenges: single-photon detection at 1.3 μm , (1.55 μm)



- (Ge), InGaAs APDs
 - Rarity et al., Cova et al., Gisin et al., [Morgan et al.](#)

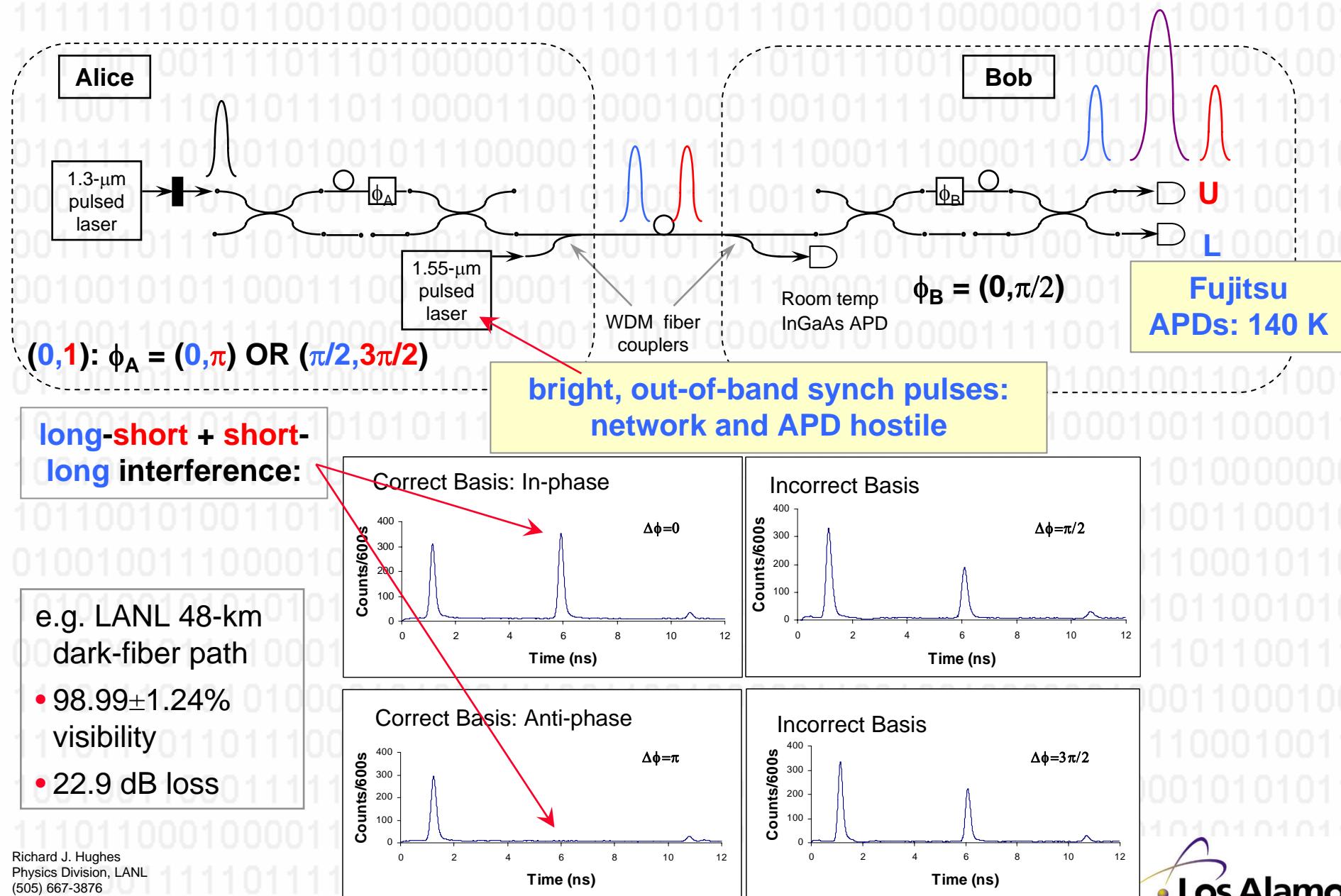
e.g. InGaAs APDs (Fujitsu)

- cooled to 140 K
- detection efficiency, time-resolution and noise **increase** with over-voltage
- 20% efficiency, 50 kHz noise
- **high noise rate can be offset by sub-ns time-resolution**

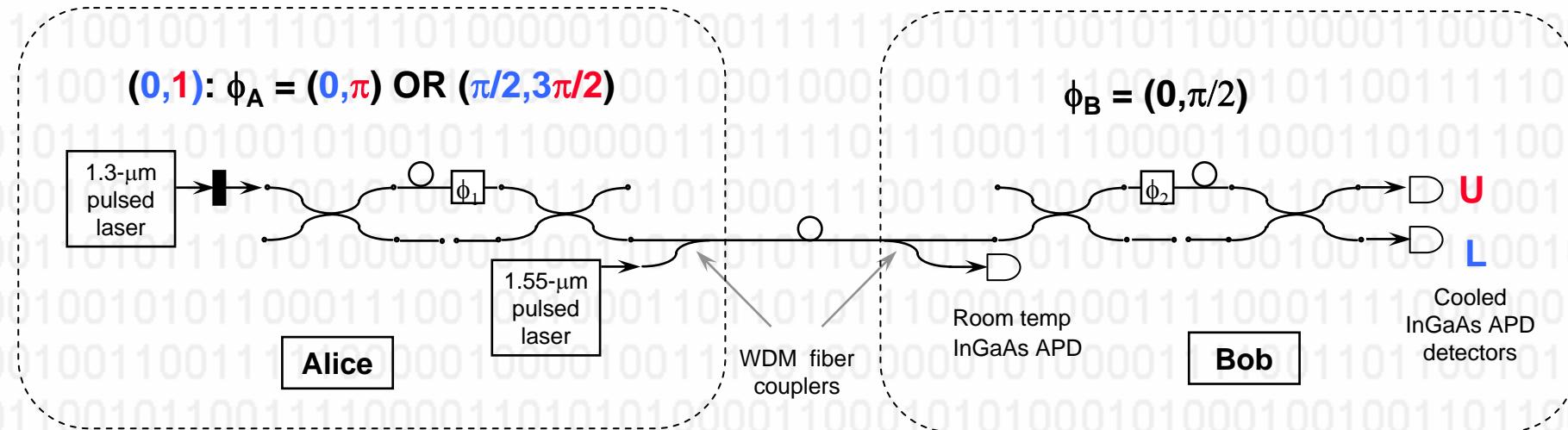


F1QKD: BB84 using (multiplexed) single-photon interference

R. J. Hughes et al., J. Mod. Opt. 47, 533 (2000)



BB84 key generation



Sample of 48-km BB84 key bits

A 00001**0**01 01111111 **1**0000**1**11 10000000 **0**111000**1** 10011110 00110101 10000111
B 00001**1**01 01111111 **0**0000**0**11 10000000 **0**011000**0** 10011110 00110101 10000111

A 000**1**0000 00**0**01000 10100010 000000**0**11 00100101 00000000 00110011 01100010
B 000**0**0000 00**1**01000 10100010 00000**1**11 00100101 00000000 00110011 01100010

- BER ~ 9.3 %; key rate ~ 20 Hz (2x B92)

Requirements for QKD in AONs

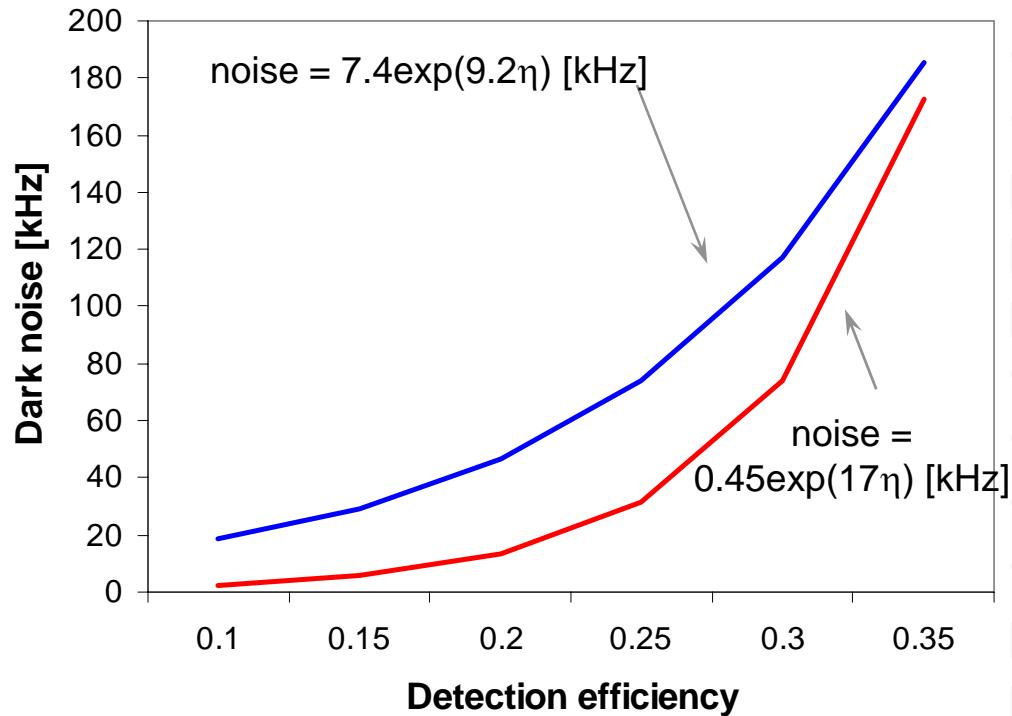
Requirement	F1/F2 limitation	F3QKD solution
“Ease of use”: focus on network, not physics	Physicist required	Engineered, automated, stable system
Multi-wavelength capable: co-existence	Fixed wavelength	Novel modular design
Network-friendly synchronization	Out-of-band bright pulses	Syntonized Rb oscillators
Accommodate path length changes	Static path length	Auto-synchronization and tuning
Background tolerant	Dark fiber	Epitaxx APDs
Clock rates < 10 MHz	Clock rates < 100 kHz	After-pulse blocking APD gates ~ 600ps
Complete protocol	—	Includes all classical elements + authentication

F3QKD Epitaxx APDs: “ease-of-use” + tolerate higher backgrounds⁸⁹

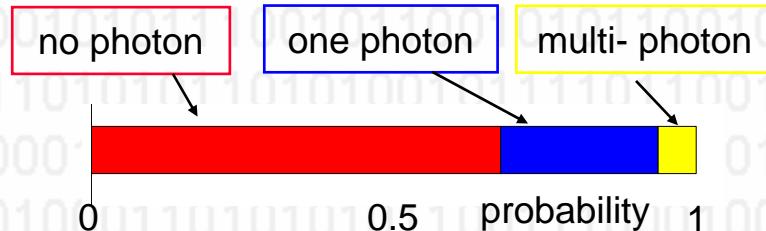
P. Hiskett

— Fujitsu 140K — Epitaxx 220K

- F1/F2QKD: Fujitsu InGaAs APDs required refrigerator to reach 140K
- Epitaxx APDs: lower dark noise for same efficiency at higher temperatures
 - accessible with TE cooling
- e.g. $\eta \sim 20\%$, dark noise
 - Fujitsu (140K) ~ 47 kHz
 - Epitaxx (220K) ~ 13 kHz
- in dark fiber
 - greater max range: 32dB loss vs 24dB
 - higher yield at given range: e.g. @20dB
 - 1.9×10^{-4} secret bits/trans bit (Epitaxx)
 - 0.8×10^{-4} secret bits/trans bit (Fujitsu)



BBBSS91 privacy amplification



Eve identifies all multi-photon signals, errors due to intercept/resend on single-photon signals

QIS&T

- today: a healthy endeavor spanning the range from basic science to emerging technology
 - potentially offering unprecedented new information assurance capabilities
- where would we like to be in 10 years?
- what will it take to get there ?
scientific, technological, infrastructure, skills (people), targeted \$, ... developments ?
- (how) will the present array of approaches help us get there ?

a Research Roadmap:

- apply some gentle direction
- describe state-of-play and likely progress
- identify opportunities and gaps + places where strategic investments would be beneficial
- an aid to the research community and a descriptive tool for program management
- a living document

A Quantum Information Science and Technology Roadmap

Part 2: Quantum Cryptography Report of the Quantum Cryptography Technology Experts Panel

“When elementary quantum systems...are used to transmit digital information, the uncertainty principle gives rise to novel cryptographic phenomena unachievable with traditional transmission media.”
Charles H. Bennett and Gilles Brassard (1984)

Disclaimer:

The opinions expressed in this document are those of the Technology Experts Panel members and are subject to change. They should not be taken to indicate in any way an official position of U.S. Government sponsors of this research.

July 19, 2004

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This document is available electronically at: <http://qist.lanl.gov>

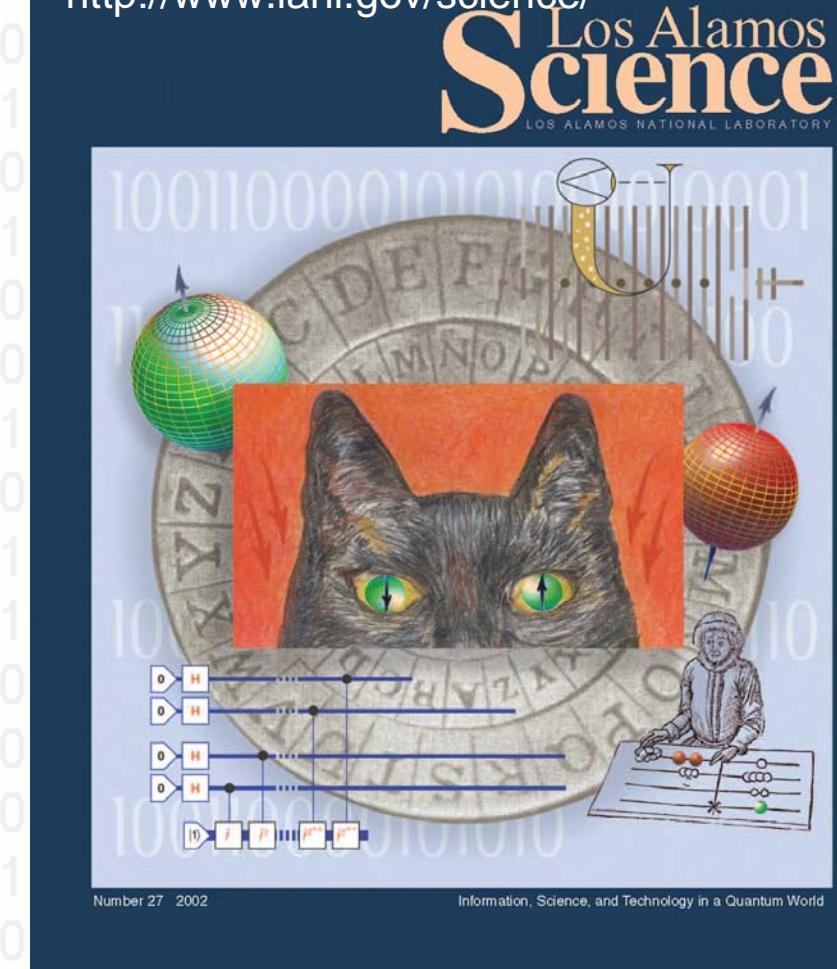
Summary

QKD is evolving from fundamental physics towards a “quantum information assurance” era

- a new tool for secure communications, enhancing conventional key management, to meet future needs
- a physical layer technology
 - co-existence with conventional optical communications ?
- **Satellite-to-ground QKD**
 - no showstoppers
- **QKD in all-optical fiber networks**

Further reading:

J. E. Nordholt & R. J. Hughes,
Los Alamos Science 27, 68 (2002)
<http://www.lanl.gov/science/>



“Information, Science and Technology in a Quantum World”